

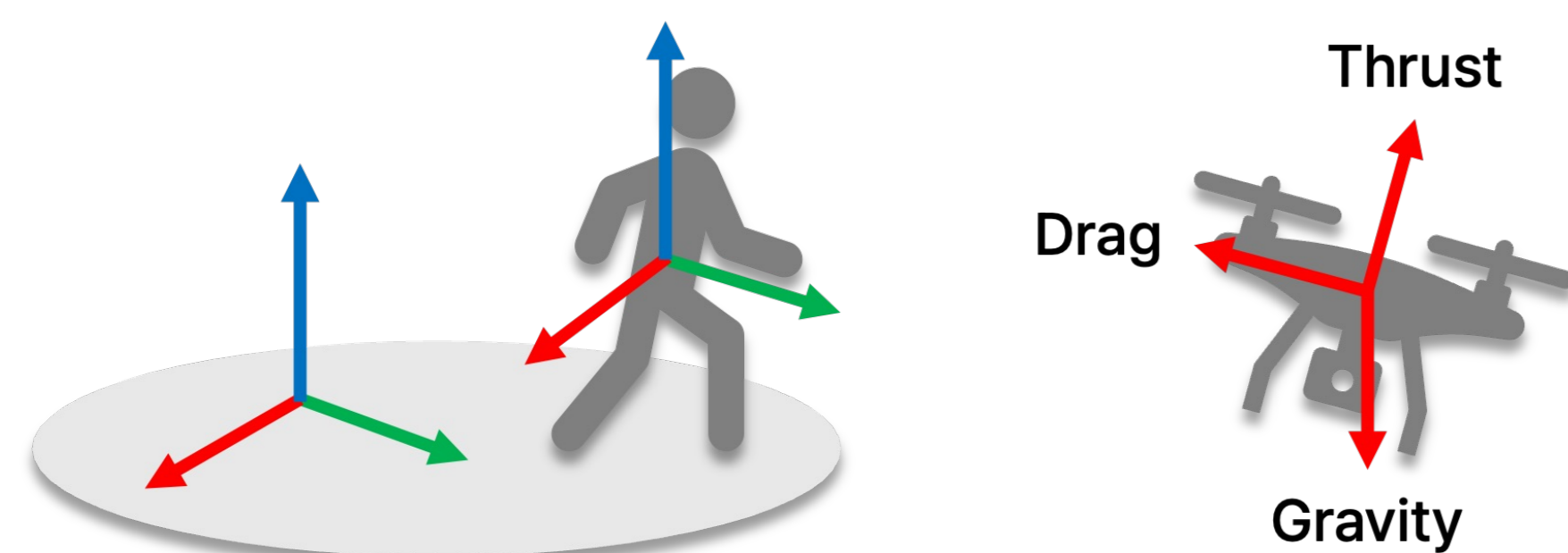
# Equivariant Neural Inertial Odometry for Microgravity Space Robotics

Sejun Ahn<sup>1</sup> Yuheng Qiu<sup>2</sup> Chanhee Park<sup>1</sup> Brian Coltin<sup>3</sup> Ryan Soussan<sup>3</sup> Pyojin Kim<sup>1\*</sup>

<sup>1</sup> Gwangju Institute of Science and Technology <sup>2</sup> Carnegie Mellon University <sup>3</sup> NASA Ames Research Center

## Background & Motivation

**Neural Inertial Odometry (NIO)** learns and predicts the translational motions from IMU-only, but existing methods rely on gravity-dependent priors inherited from terrestrial settings.



## On Earth: Gravity as a strong motion prior

**Pedestrian** – gravity as a **coordinate reference**

- Horizontal dominant motion: walk on the ground
- Align to gravity: Gravity-Aligned Coordinate Frame

$${}^G \mathbf{a} = \mathbf{R} {}^B \mathbf{a}, {}^G \boldsymbol{\omega} = \mathbf{R} {}^B \boldsymbol{\omega}$$

→ Reduces learning hypothesis space from SO(3) to SO(2)

**Drone-UAV** – gravity as a **feature observability** source

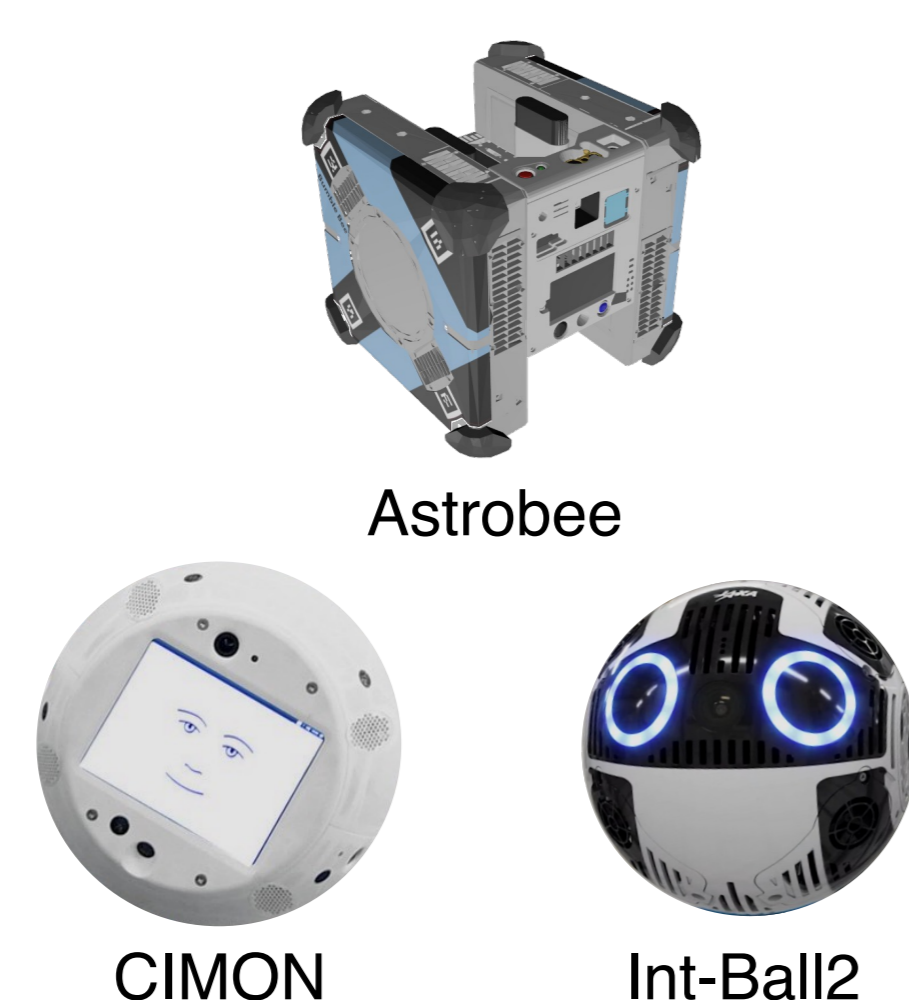
- Attitude coupled motion: increase tilt for thrust
- Embed attitude via gravity in body frame representation

$${}^B \mathbf{a} = \frac{{}^B \mathbf{F}_{net}}{m} + \mathbf{R}^T {}^G \mathbf{g}$$

→ Enhances feature observability of the network

## In Space: Gravity-dependent priors no longer hold

ISS free-flyers operate in **microgravity**, with fully arbitrary attitude, holonomic dynamics, and unconstrained 3D motion



- **Gravity-induced priors are inapplicable to ISS free-flyers**
- **No prior NIO has been tailored to microgravity settings**

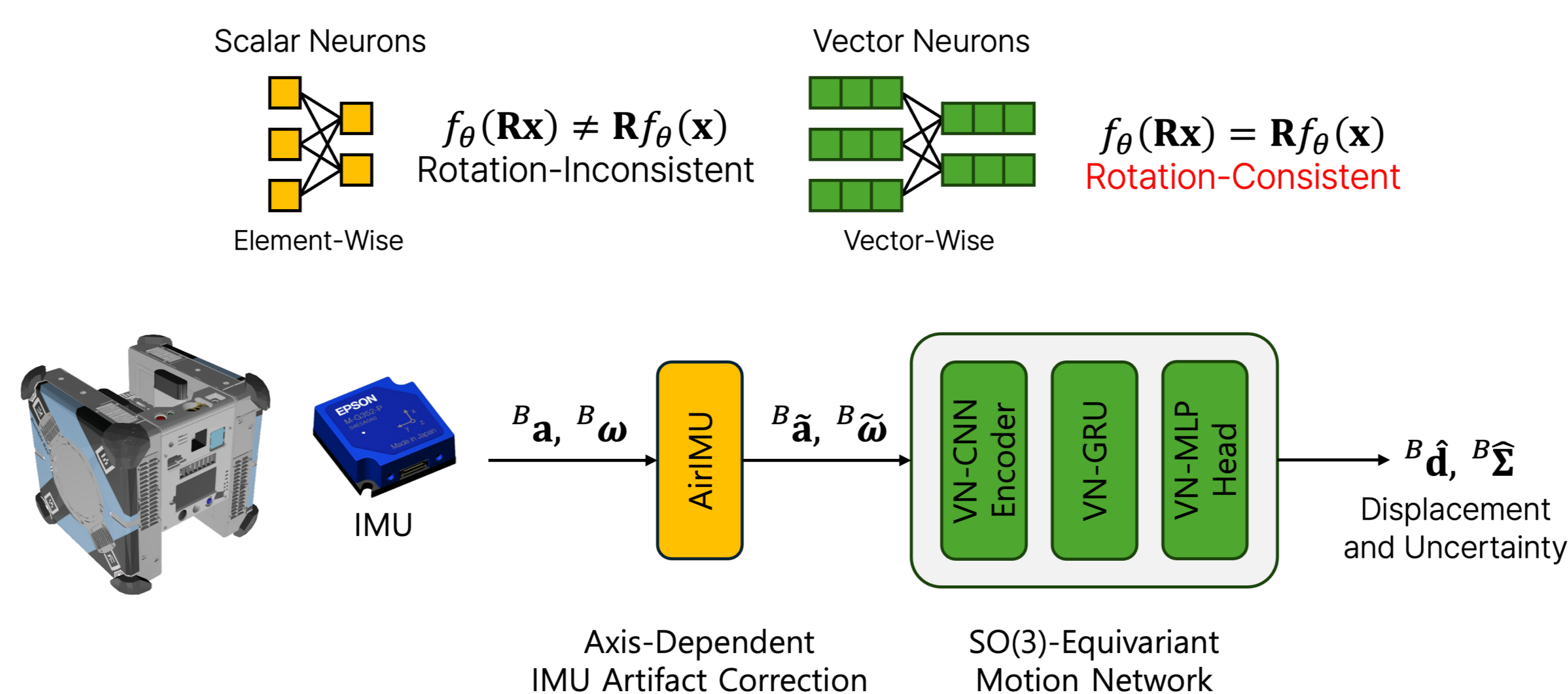
## Contribution

- Proposes a **microgravity-tailored NIO** framework for unconstrained 3D free-flyer motion.
- Encodes **SO(3)-equivariance** as an architectural inductive bias for rotation-consistent motion prediction.
- Demonstrates **improved accuracy and generalization** on unseen Astrobee simulation trajectories.

## Methodology

**SO(3)-Equivariance as a Principled Inductive Bias**

- Encodes rotational symmetry using Vector Neurons [1], rotation-consistent predictions under arbitrary 3D rotations.



### Ⓢ Axis-Dependent IMU Artifact Correction

- Learns and corrects asymmetric IMU bias/noise.
- Produces corrected IMU measurements for equivariant motion learning.

$${}^B \tilde{\mathbf{a}} = {}^B \mathbf{a} + {}^B \hat{\boldsymbol{\sigma}}_{acc}, {}^B \tilde{\boldsymbol{\omega}} = {}^B \boldsymbol{\omega} + {}^B \hat{\boldsymbol{\sigma}}_{gyro}$$

### Ⓢ SO(3)-Equivariant Motion Learning

- Uses Vector Neuron-based 1D-CNN/GRU/MLP layers.
- Predicts **displacement** and corresponding **uncertainty** in an SO(3)-equivariant manner.

$$\hat{\mathbf{d}}(\mathbf{R}\mathbf{x}) = \mathbf{R}\hat{\mathbf{d}}(\mathbf{x}), \hat{\boldsymbol{\Sigma}}(\mathbf{R}\mathbf{x}) = \mathbf{R}\hat{\boldsymbol{\Sigma}}(\mathbf{x})\mathbf{R}^T$$

## Experimental Result

### Dataset

- Astrobee Robot Software Simulation Dataset
- 41 sequences with a total duration of 315 minutes

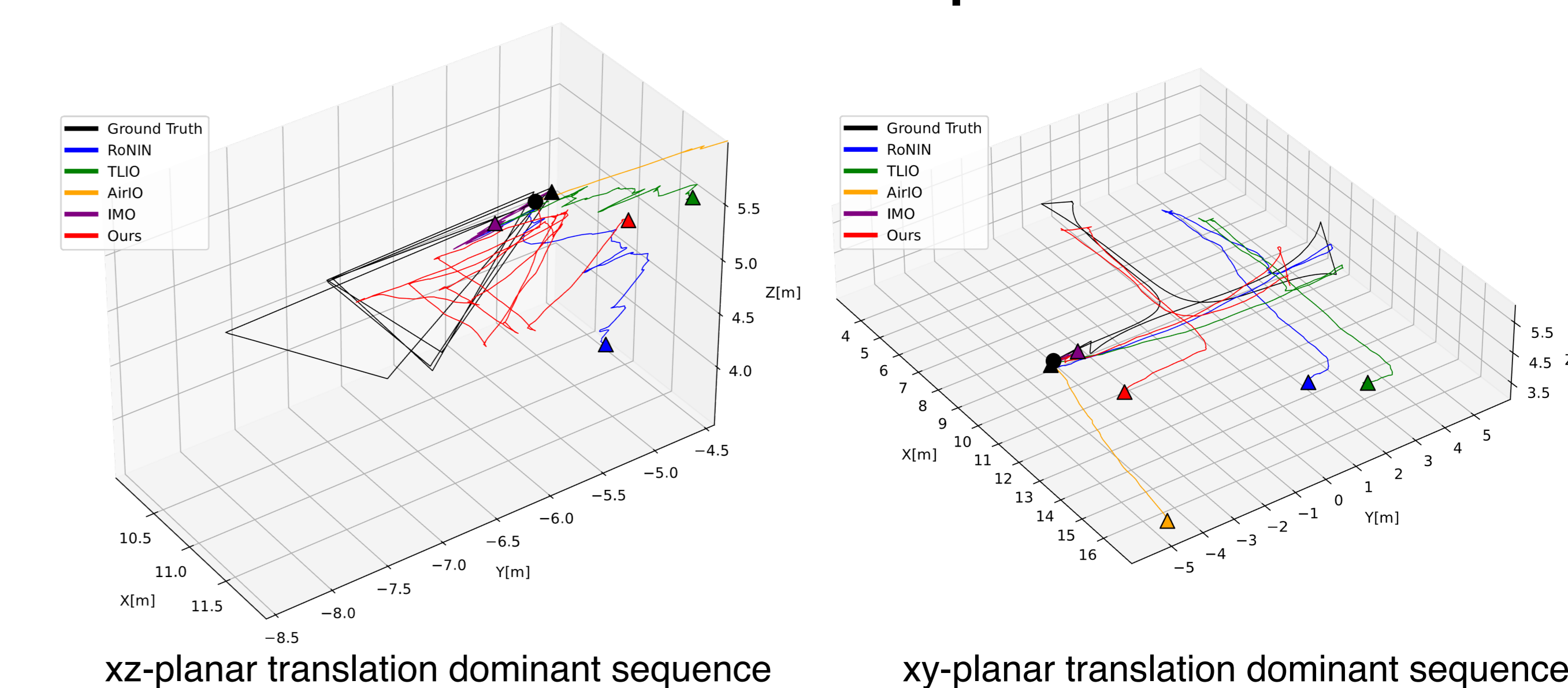
### Metric

- RMSE ATE (Absolute Translation Error) [m]
- RMSE RTE (Relative Translation Error) @ 5s [m]

\*Leverage ground-truth orientations for all methods

Sequence	Metric	RoNIN	TLIO	AirIO	IMO	Ours
Seen	ATE	2.3639	<u>2.2911</u>	3.0095	2.7928	<b>0.8335</b>
	RTE	0.2560	<u>0.2424</u>	0.2756	0.3012	<b>0.0876</b>
Unseen	ATE	<u>2.3859</u>	2.5291	3.2572	2.9146	<b>1.1413</b>
	RTE	0.2177	<u>0.2139</u>	0.2590	0.2687	<b>0.1204</b>

### Qualitative Results on Unseen Sequences



## Conclusion & Future Work

- Microgravity breaks gravity-induced priors of terrestrial NIO.
- SO(3)-equivariance serves as a principled inductive bias for microgravity NIO, improving accuracy and generalization.

### Future Work

- Evaluation on real-world Astrobee ISS dataset [3]
- IMU Sim-to-Real Domain Transfer
- Attitude estimation using IMU-only under microgravity

- [1] Deng, Congyue, et al. "Vector neurons: A general framework for so (3)-equivariant networks." *Proceedings of the IEEE/CVF international conference on computer vision*. 2021.  
 [2] Qiu, Yuheng, et al. "Airimu: Learning uncertainty propagation for inertial odometry." *arXiv preprint arXiv:2310.04874* (2023).  
 [3] Kang, Suyoung, et al. "Astrobee iss free-flyer datasets for space intra-vehicular robot navigation research." *IEEE Robotics and Automation Letters* 9.4 (2024): 3307-3314.